Exploring the dimensions of metapopulation persistence: a comparison of structural and temporal measures

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Abstract

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The spatial arrangement of habitat patches in a metapopulation, and the dispersal connections 2 among them, influence metapopulation persistence. Metapopulation persistence emerges from 3 a dynamic process, namely the serial extinctions and recolonizations of local habitat patches, 4 while measures of persistence are typically based solely on structural properties of the spatial 5 network (e.g., spatial distance between sites). Persistence estimators based on static properties 6 may be unable to capture the dynamic nature of persistence. Understanding the shape of the 7 distribution of extinction times is a central goal in population ecology. Here, we examine 8 the goodness of fit of the power law to patch persistence time distributions using data on a 9 foundational metapopulation system – the Glanville fritillary butterfly in the Åland islands. 10 Further, we address the relationship between structural measures of metapopulation persistence 11 (i.e., metapopulation capacity) and our temporal distributional fits to patch persistence times 12 based on a power law. Patch persistence time distributions were well fit by a power law for the 13 majority of semi-independent networks. Power law fits to persistence time distributions were 14 related to metapopulation capacity, linking structural and temporal measures of metapopulation 15 persistence. Several environmental variables and measures of network topology were correlated 16 with both measures of metapopulation persistence, though correlations tended to be stronger for 17 the structural measure of metapopulation persistence (i.e., metapopulation capacity). Together, 18 our findings suggest that persistence time distributions are useful dynamic properties of metapopulations, 19 and provide evidence of a relationship between metapopulation structure and metapopulation 20 dynamics. 21

Introduction

Habitat fragmentation reduces patch size leading to smaller local populations that are at greater 23 risk of stochastic extinction. Dispersal between fragmented suitable habitat patches is therefore 24 essential to maintain the network of small populations i.e., the metapopulation (Hanski, 1999; 25 Hanski and Gilpin, 1991). A body of theory has been developed to describe threshold conditions 26 for metapopulation persistence (Keymer et al., 2000), the influence of dispersal on metapopulation 27 dynamics (Doebeli, 1995; Holland and Hastings, 2008; Vuilleumier et al., 2010), and the dependence 28 of persistence on the spatial distribution of habitat patches (Ovaskainen and Hanski, 2003). 29 Metapopulation persistence estimators attempt to quantify the threshold after which colonization 30 and dispersal are unable to maintain patch occupancy, leading to metapopulation collapse. 31 The initial development of metapopulation theory drew heavily on the Levin's model, which 32 tracks species occurrences among patches regardless of spatial location or size of habitat patches 33 (Levins, 1969). Building on this, Hanski (1994) developed a spatially-explicit metapopulation 34 model which incorporated variation in habitat patch size and explicitly considered the role 35 of space. Through this work, the development of a persistence measure called *metapopulation* 36 capacity was developed (Hanski and Ovaskainen, 2000; Ovaskainen and Hanski, 2001). 37

We use *metapopulation capacity* to measure metapopulation persistence based on the spatial 38 distribution of habitat patches and dispersal links between them (Hanski and Ovaskainen, 2000; 39 Ovaskainen and Hanski, 2001). This information is contained within the landscape matrix 40 (M), which describes the putative dispersal links between all habitat patches (Hanski, 1999; 41 Ovaskainen and Hanski, 2001). While the landscape matrix is often constructed in the absence 42 of a dynamic model, the original formulation of metapopulation capacity (λ) was based on 43 a metapopulation model (Hanski and Ovaskainen, 2000). Previous work has suggested that 44 metapopulation capacity (λ) is associated with equilibrium patch occupancy when habitat patches 45 are of good quality and are aggregated in space (Hanski and Ovaskainen, 2000; Visconti and 46 Elkin, 2009), suggesting a role for both environmental quality and spatial network structure 47 on metapopulation capacity (Hanski et al., 2017). Conservation and management decisions have 48

⁴⁹ been informed by metapopulation capacity (Hanski, 2011; Hanski and Thomas, 1994; McCullough, ⁵⁰ 1996), as it is used to estimate long term metapopulation persistence (Hanski and Ovaskainen, ⁵¹ 2000). Similar eigenvalue-decompositions have been used to estimate *a*) epidemic thresholds in ⁵² social contact networks (Saha et al., 2015), *b*) nestedness in bipartite networks (Staniczenko et al., ⁵³ 2013), *c*) the basic reproductive number (R_0) of infectious disease given infection time series ⁵⁴ (Diekmann et al., 2010), and *d*) early warning signals of spatial population collapse (Chen et al., ⁵⁵ 2019).

Previous efforts to link metapopulation persistence measures derived from the spatial distribution 56 of patches to the resulting dynamics have largely focused on metapopulation persistence in an 57 absolute sense, quantifying the number of times in model simulations the metapopulation goes 58 extinct (Kleinhans and Jonsson, 2011). Other efforts have defined persistence using measures 59 related to extinction-colonization ratios or mean species occupancy (i.e., fraction of patches where 60 the species is found). These measures often define metapopulation persistence as either the 61 probability that the entire metapopulation goes extinct, or the mean species occupancy over 62 some time window (Johst et al., 2002; Molofsky and Ferdy, 2005). The first is a coarse measure, 63 and is difficult to empirically test, given the need for a metapopulation extinction event, which 64 tend to be rare and not easily replicated. The second measure may fail to capture rescue effects 65 or transient patch occupancy followed by local extinction, that may serve as an early warning 66 signal of metapopulation collapse (but see Holmes et al. (2020)). Ideally, a measure of persistence 67 at the metapopulation scale would incorporate information on each habitat patch explicitly, both 68 in terms of mean and variation in climatic conditions. For instance, Increasing climatic variability 69 may drive metapopulation dynamics near extinction thresholds, even those as established as the 70 Glanville fritillary metapopulation in the Åland islands (van Bergen et al., 2020). 71

In population ecology, a body of theory related to the distribution of extinction times for
single populations has been developed (Drake, 2006, 2014). That is, without immigration or
emigration, what does the distribution of extinction times look like for a set of populations?
A common observation is that this distribution has a heavy tail, where most populations go

extinct in a relatively short time, but few populations exist for far longer (Drake, 2014). In 76 the context of metapopulations, the distributional fit to patch extinction times - which are 77 equivalent to *persistence times* – may provide information on the metapopulation as a whole while 78 directly incorporating patch level dynamics (Bertuzzo et al., 2011). This approach requires either 79 simulated or empirical data on patch persistence times to generate the persistence estimate. That 80 is, estimating the distribution of persistence times for each patch in the network could provide 81 insight into the presence of long-persisting nodes, and those which go extinct but recolonize 82 quickly. One such distributional fit proposed recently is the power law (Bertuzzo et al., 2011), 83 where some quantity *x* is drawn from a probability distribution $p(x) \propto x^{-\alpha}$. The interpretation 84 of α then becomes important, as this scaling parameter starts to address the heavy-tailed nature 85 of the distribution of empirical values of x. Power law relationships are commonly found in 86 natural systems, such as the bivariate scaling of the number of species with increasing geographic 87 area (the species-area relationship; Martín and Goldenfeld (2006)). Power law relationships 88 in frequency distributions, as examined here, are equally common in ecological studies of the 89 distribution of species body sizes (Morse et al., 1985), abundance estimates (Keitt and Stanley, 90 1998), and vegetation patch size (Kéfi et al., 2007), as reviewed in White et al. (2008). 91

Here, the parameter α estimates the shape of the long tail of persistence times, with smaller 92 α values corresponding to heavier tails. This means that large α values correspond to more 93 extreme decay rates in persistence times (x), with very few long persistent patches, indicative of 94 high extinction and rapid recolonization of habitat patches. That is, the probability density of 95 persistence times (*x*) are proportional to $x^{-\alpha}$. As such, there are two clear possible relationships 96 between metapopulation capacity (λ) and persistence time distributions (α). First, a positive 97 relationship may emerge between persistence time distributional fits (α) and metapopulation 98 capacity (λ) if long-term persistent habitat patches drive metapopulation persistence. These 99 long-term persistent patches would lead to a heavier-tailed distribution of persistence times, 100 reducing the α value. On the other hand, metapopulations are characterized by rapid extinction 101 and re-colonization dynamics, and these dynamics may be indicative of a persistent metapopulation. 102 Thus, a second possibility is that we may expect a negative relationship between metapopulation 103

¹⁰⁴ capacity (λ) and persistence time fits (α). This would suggest that short-lived, but quickly ¹⁰⁵ recolonized habitat patches, are a signature of a persistent metapopulation.

Apart from implications to metapopulation persistence, the α parameter may also be useful 106 in differentiating different *types* of metapopulations (as identified in Harrison and Taylor (1997)). 107 This is because the balance between ephemeral and persistant habitat patches can inform metapopulation 108 structure. For instance, mainland-island metapopulations would be expected to have a smaller α 109 value, driven by the long-persisting source patches, while classic metapopulations would have 110 larger α values due to the common extinction and colonization events reducing the probability 111 of long-persisting patches. Finally, understanding the differences in power law relationships for 112 unconnected populations (Drake, 2006, 2014) – corresponding to non-equilibrium metapopulations 113 as defined in Harrison and Taylor (1997) – and connected metapopulations can provide insight 114 into the role of dispersal and rescue effects on persistence. 115

How well do structural (metapopulation capacity) or temporal (persistence time distributions) 116 measures of metapopulation persistence describe metapopulation dynamics, given that they both 117 putatively quantify metapopulation persistence? A common assumption of many metapopulation 118 studies is that structural properties of the metapopulation (e.g., metapopulation capacity) capture 119 dynamic processes (Hanski and Ovaskainen, 2000). That is, a positive relationship between 120 structural (metapopulation capacity) and temporal (persistence time distributional fit) measures 121 of metapopulation persistence should exist. Further, the relationships between environmental 122 and topological aspects of the metapopulation should correlate well with both measures of 123 metapopulation persistence, though perhaps with different strength. We would expect that 124 measures of spatial network topology (e.g., connectance) should strongly correlate with metapopulation 125 capacity (λ), as the both measures are based on the same data (i.e., the landscape matrix **M**). 126 However, factors influencing distributional fits to persistence times should correspond more to 127 local environmental conditions and resource availability, as measures of metapopulation persistence 128 that are based on local dynamics are likely to be more sensitive to local environmental conditions 129 than measures based on metapopulation structure alone. 130

Here, we examine the relationship between structural (metapopulation capacity) and temporal 131 (persistence time distributions) measures of metapopulation persistence, providing a link between 132 the geographic distribution of habitat patches and the resulting temporal metapopulation dynamics. 133 Further, we explore power law scaling relationships in patch persistence times, providing evidence 134 that interconnected populations have similarly heavy-tailed persistence (or extinction) time distributions 135 compared to isolated replicated populations (Drake, 2014). Using a long-term sampling effort of 136 Melitaea cinxia populations distributed across meadow habitats in the Åland islands sampled over 137 20 years, we demonstrate a positive relationship our measures of metapopulation persistence for 138 a set of 88 semi-independent spatial networks (also referred to as *network components*). Further, we 139 investigate how environmental and topological aspects of the spatial network are related to both 140 measures of metapopulation persistence. Environmental characteristics, such as mean resource 141 availability and grazing pressure, were largely unrelated to either measure of metapopulation 142 persistence, while topological properties – such as modularity and the number of patches in the 143 network – were strongly correlated to both measures of metapopulation persistence. Together, 144 this provides a link between structural and temporal measures of metapopulation persistence, 145 and demonstrates clear relationships between aspects of the landscape matrix and the resulting 146 measures of metapopulation persistence, either measured using putative dispersal connections, 147 or through a power law scaling relationship in patch persistence times. 148

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Methods

Glanville fritillary metapopulation data

In the Åland islands, a set of approximately 4500 habitat patches have been monitored since 1993. Here, we use data from the Fall surveys of the Glanville fritillary butterfly (*Melitaea cinxia*) nests sampled annually between 1993 and 2016 (Ojanen et al., 2013). Each habitat patch was occupied by at least one of two host plant species – either *Plantago lanceolata* or *Veronica spicata* – which serves as a food and oviposition resource for *M. cinxia*. Habitat patches exist in a mosaic of inhospitable habitat, and links between habitat patches represent potential dispersal pathways. ¹⁵⁷ We examined a subset of 2249 habitat patches which contained sufficient data, leading to the ¹⁵⁸ creation of 88 semi-independent networks (SINs). Each SIN has been identified to be a cluster of ¹⁵⁹ patches where most of the dispersal dynamics are assumed to take place within the SIN (Hanski ¹⁶⁰ et al., 2017). This allows for a certain degree of replication of metapopulations in a natural setting.

Each of these 88 SINs is treated as a metapopulation, and represent a wide range of metapopulation
 structures. The number of habitat patches in the SINs ranges from 2 to 147, and patch sizes
 ranged from 0.001 to 10.2 hectares. Patch size within SINs tends to be quite variable, with
 coefficient of variation (mean divided by standard deviation) varying between 0.03 and 0.34.
 This range of metapopulation structures provides both challenge and opportunity to examine
 the relationship between metapopulation capacity and persistence time distributions.

R code and data to reproduce the analyses is provided at
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169

Metapopulation capacity: the structural persistence measure

Metapopulation capacity estimates the ability of a metapopulation to support long-term persistence 170 of a given species (Hanski and Ovaskainen, 2000) based on the distances among habitat patches 171 in the spatial network. Specifically, metapopulation capacity (λ) is the dominant eigenvalue 172 of the landscape matrix M, which is a square matrix describing dispersal connections among 173 habitat patches. Concretely, the diagonal elements of the landscape matrix M are zero, and 174 off-diagonal elements estimate dispersal probabilities between two habitat patches i and j that 175 are some distance d_{ii} away from one another. The landscape matrix **M** is estimated for each SIN, 176 assuming that an exponential decay function as the basis for dispersal (Equation 1), based on 177 previous research in this system (Hanski et al., 2017). 178

$$\mathbf{M} = A_i^{x+\gamma} e^{-\epsilon d_{ij}} A_j^{\psi} \tag{1}$$

In the original formulation, entries of the landscape matrix (\mathbf{M}) were defined by including 179 patch area (A_i and A_j) as a surrogate measure of carrying capacity. However, non-linear relationships 180 and density-dependent dispersal probabilities may influence the relationship between patch area 181 and population size (and subsequent dispersal probabilities). To address this, we formulate the 182 **M** matrix with the inclusion of patch area, assuming that immigration (γ), extinction (x), and 183 emigration (ψ) are functions of patch area and collectively balance (i.e., $x + \gamma = \psi = 0.25$; 184 Hanski et al. (2017)). We examine the influence of excluding patch area in the calculation of the 185 M matrix in the Supplemental Materials. 186

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Persistence time distributions: the temporal persistence measure

We examine power law scaling relationships in persistence time distributions obtained for each 188 semi-independent network (SIN). For a given SIN, we calculated persistence times for each patch 189 over the course of the study period (1993-2016). Persistence was defined as any consecutive 190 period that a given patch was occupied, taking values between 1 to 24. While previous studies 191 have developed approaches to address the potential left and right censoring of the time series 192 data (i.e., patches may persist for longer than 24 years. Due to the extremely dynamic nature of 193 the SINs examined – mean patch persistence time across SINs ranged from 1 to 4.8 – we do not 194 attempt to extrapolate to unsampled periods. No patch was occupied for every sampling period, 195 and only 4 out of the 2249 habitat patches in the 88 SINs examined persisted for 23 years. 196

¹⁹⁷. Because of the dynamic nature of these metapopulations, patches could contribute multiple ¹⁹⁸ persistence times to the distribution. This means that patches that go extinct and are recolonized ¹⁹⁹ contribute more data to the distribution. However, it is the persistent patches that drive the ²⁰⁰ heavy tail of the persistence time distribution, as well as the corresponding value of α . This α is ²⁰¹ estimated using maximum likelihood, following the equation

$$\hat{\alpha} = 1 + n \left[\sum_{i=1}^{n} log \left(\frac{x_i}{x_{min} - 0.5} \right) \right]^{-1}$$
 (2)

²⁰². Here, we use the hatted symbol ($\hat{\alpha}$) to denote α as estimated from data. The parameter x_{min} ²⁰³ is the lower bound of persistence times x where the power law can be fit to the data. Each ²⁰⁴ SIN has a fit x_{min} and α value. In the Supplemental Materials, we explore the distribution ²⁰⁵ and relationship between x_{min} and α values fit for each SIN. Power law distributions were fit ²⁰⁶ using the poweRlaw package in R, following the bootstraping procedure to account for parameter ²⁰⁷ uncertainty (Gillespie, 2015). Further, goodness of fit to the power law distribution was determined ²⁰⁸ via bootstrapping following Clauset et al. (2009).

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Relating metapopulation persistence measures

We related metapopulation capacity (λ) to the power law fit parameter (α) characterizing the tail 210 of the persistence time distribution for each SIN using a Spearman's rank correlation to account 211 for a potentially non-linear relationship. Larger values of metapopulation capacity are indicative 212 of a greater chance of species persistence in the metapopulation. Larger values of persistence 213 time fits (α) correspond to a faster decay in persistence times, and an increased number of 214 short-lived but quickly recolonized patches. Assuming that consistently colonized patches are a 215 sign of network-level persistence, a negative relationship between metapopulation capacity (λ) 216 and persistence time fits (α) is expected. However, if we interpret the rapid recolonization and 217 extinction of patches as a signature of a dynamic, but persistent, metapopulation, a positive 218 relationship may emerge. 219

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Correlates of metapopulation persistence measures

Numerous environmental covariates may influence habitat patch quality, which affects subsequent colonization and extinction dynamics (Fleishman et al., 2002; Thomas, 1994). Given that metapopulation capacity does not directly incorporate information on variation in patch quality, but that the persistence time distributional fit does likely reflect patch quality, we would expect that environmental conditions would most strongly correlate with the persistence time distributional fits (α).

Patch area was estimated during sampling, with the median patch area being approximately 226 0.6 ha, and the majority of habitat patches smaller than 2 ha. The two common host plants of M. 227 cinxia are Plantago lanceolata and Veronica spicata. We quantified resource availability as the sum 228 of abundance of these two host plants based on an ordinal scale between 0 and 3 for each species, 229 with larger values corresponding to a greater plant abundance (Ojanen et al., 2013). Previously, 230 the summed abundance of these two host plants has been predictive of colonization, extinction, 231 and occupancy in the Aland islands (Dallas et al., 2019). For each SIN, we calculated the mean 232 resource abundance and the variance in resource abundance. Grazing pressure was estimated 233 as the estimated fraction of the habitat patch subjected to grazing based on observations of 234 damaged plants. Plantago lanceolata, which serves as the dominant host plant through much of 235 the Aland island system, is infected by a powdery mildew pathogen (*Podosphaera plantaginis*; 236 Tollenaere et al. (2014)), which reduces plant resource quality and subsequent overwintering 237 survival and emergence of larvae in the spring (van Nouhuys and Laine, 2008). Mildew infection 238 was estimated as the mean fraction of patches within each SIN where the mildew pathogen was 239 present across each sampling period. 240

Aspects of the structure of each SIN may be related to metapopulation persistence. These 241 include the number of habitat patches in the SIN, as well as several measures of spatial network 242 structure. For instance, the tendency of patches to cluster into small groups, forming smaller 243 communities in which dispersal is expected to be stronger, is likely related to spatial network 244 persistence (Fletcher Jr et al., 2013). To quantify this, we used a series of measures which 245 capture different aspects of community formation. All measures were performed on the weighted 246 landscape matrix M for each SIN, where weights were the dispersal probabilities generated from 247 the negative exponential dispersal kernel described above. 248

First, we estimated modularity of the network by first identifying clusters within each SIN
 using the random walk approach of Pons and Latapy (2005), and then quantifying the tendency
 of these identified communities to result in a modular network, estimated using the igraph R
 package (Csardi and Nepusz, 2006). Second, we calculated the hub score of the landscape matrix

M (Kleinberg, 1999), which is nearly identical to calculation as metapopulation capacity, and is 253 the dominant eigenvalue corresponding to the principal eigenvector of $M \times t(M)$ (the landscape 254 matrix M multiplied by its transpose). Lastly, we measured a weighted form of transitivity – 255 also referred to as the 'clustering coefficient' – which quantifies the degree of spatial aggregation 256 in habitat patches within a given SIN (Barrat et al., 2007). All of these measures attempt to 257 address the distribution of patches in each SIN with respect to their estimated dispersal links 258 estimated in Equation 1. Consequently, it is important to note that estimates of network structure 259 described above will be sensitive to the formation of the landscape matrix (M). Given that only 260 metapopulation capacity (λ) uses information contained in the landscape matrix (M), we would 261 expect metapopulation capacity to be more strongly related to these aspects of dispersal network 262 structure than persistence time distributional fits. 263

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Results

Some SINs (n = 27) did not have enough data to compute distributional fits to the persistence 265 times (α). For the SINs that did have enough data, the best fit values of x_{min} and α were quite 266 variable (see Supplemental Material, Figures A2 - A4). The majority of α values were between 267 2 and 3, supporting previous observations (Clauset et al., 2009). Based on bootstrap tests, there 268 is evidence that the power law is the best fit distribution for 87% (n = 53 of the 61 SINs) of the 269 persistence time distributions, based on a significance level of 0.05 following the procedure of 270 Clauset et al. (2009). The *p*-value generated from this test can be used as a measure of plausibility 271 of the fit between empirical data and power law fit. It is not a test of the goodness-of-fit of the 272 power law directly, as p > 0.05 cannot be interpreted as support of the power law fit, while p < 100273 0.05 would suggest that the power law is not the best fit. 274

There was no apparent spatial pattern in power law fit parameter (α) to the persistence time distribution (Figure 1d) or metapopulation capacity (Figure 1b) of each SIN, though clear variation was observed in both fit persistence time distributions ($\alpha \in [1.86 - 5.04]$) and metapopulation capacities ($\lambda \in [0.003 - 1.56]$). Further, there was no significant relationships observed between either metapopulation persistence measure – metapopulation capacity (λ) or persistence time distributional fits (α) – to either mean patch persistence times or mean fraction of occupied patches (Figure 2). However, the two measures of metapopulation persistence were strongly related to one another (Figure 3), suggesting a clear link between the two measures of metapopulation persistence.

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Correlates of metapopulation persistence measures

We then related a set of environmental (e.g., mean resource availability) and network (e.g., 285 number of habitat patches) to both persistence time distributions (α) and metapopulation capacities 286 (λ) for each of the studied SINs. We hypothesized that variables not captured in the landscape 287 matrix may be better described by persistence time distributions, while structural properties 288 of the landscape matrix (M) may be more strongly related to metapopulation capacity. We 289 found that environmental variables and measures of spatial network structure tended to be more 290 strongly related to metapopulation capacity (Figure 4). The exception to this was the mean 291 fraction of patches infected by a mildew pathogen, which was negatively related to persistence 292 time distributional fits, while we failed to detect any relationship with metapopulation capacity 293 (Figure 4). Together, we found strong relationships between the metapopulation capacity and 294 both measures of dispersal network structure and local environmental covariates (Figure 4), but 295 generally slightly weaker relationships for the distributional fits to patch persistence times. 296

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Discussion

The majority of patch persistence time distributions were best fit by the power law, clarifying a link between extinction time distributions from population ecology – as well as other power law relationships (Marquet et al., 2005) – and patch-scale persistence time distributions of interconnected populations. Weak correlations between composite measures of each SIN (mean persistence time and mean occupancy) and metapopulation capacity belie the significant positive relationship between structural (metapopulation capacity) and temporal (persistence time distributional fit)

measures. This provides evidence for a clear relationship between the two measures of metapopulation 304 persistence, despite the two measures using information on *either* static network topology (as 305 estimated in the landscape matrix M) or temporal data on patch persistence times, effectively 306 linking two approaches to the estimation of metapopulation persistence. Further, several environmental 307 and network structural variables were correlated with both metapopulation persistence measures. 308 However, we found little support for the hypothesis that persistence time distributional fits would 309 be more closely related to aspects of patch quality which are not considered in the calculation of 310 metapopulation capacity. This suggests that – at least in the Åland island system – persistence 311 time distributions for each SIN are largely unrelated to habitat variables at the scale of the entire 312 metapopulation. Taken together, this suggests a strong link between spatial network topology 313 and the resulting dynamics, provides evidence for the use of persistence time distributions to 314 understand metapopulation persistence, and extends theory related to heavy-tailed population 315 extinction time distributions to understanding interconnected populations and metapopulations. 316

Patch persistence time distributions characterized by high values – corresponding to dynamic 317 metapopulations where rapid colonization and extinction events shorten the tail of the persistence 318 time distribution – were associated with high metapopulation capacity (α). This suggests that 319 the existence of long-term persistent patches may not be a signature of overall metapopulation 320 persistence. The opposite appears to be the case, where metapopulations composed of patches 321 which rapidly become extinct and are rapidly recolonized tend to be the most structurally 322 persistent (based on metapopulation capacity). This finding may be influenced by species traits 323 such as dispersal ability and survival. However, a species which colonizes a set of habitat 324 patches and persists in each patch is not a true metapopulation (Harrison and Taylor, 1997). 325 However, the persistence time distribution may be useful outside of these *true* metapopulations, 326 as understanding the distribution of extinction times is central to population ecology (Drake, 327 2006, 2014). Further, the persistence time distribution may signal metapopulation "type" (as 328 defined in Harrison and Taylor (1997)), as mainland-island metapopulations would have a longer 329 tailed persistence time distribution relative to the classical metapopulation or patchy population. 330

We failed to detect strong relationships between persistence time distributional fits and local-scale 331 environmental variation in the Åland island metapopulation. The lack of relationship between 332 persistence time distributional fits and patch quality variables might simply be a function of the 333 inherent variation in persistence time distributions and the subsequent power law distributional 334 fits. This is because habitat patch persistence may largely be a stochastic process, in which 335 patches go extinct and are recolonized often. This, in turn, strongly influences the distribution 336 of persistence times and resulting distributional fits. Despite the weak relationships between 337 patch quality and persistence time distributions, we found strong relationships between network 338 structure (e.g., modularity) and both measures of metapopulation persistence, suggesting a signal 339 of the effect of landscape matrix structure on resulting metapopulation persistence. Lastly, 340 metapopulation capacity was found to be positively related to local-scale habitat covariates 341 (e.g., mean patch area), even when patch area was not used to quantify dispersal links in the 342 metapopulation (Figure A8). These correlations could not be explained by the associations 343 between patch area, resource abundance, and grazing pressure (Figure A9) alone (see Supplemental 344 Materials for further discussion). Spatial autocorrelation in local environmental conditions which 345 scale up to the network level might result in correlations between environmental covariates and 346 metapopulation capacity as well. Examining other metapopulation systems may provide insight 347 into the relative strength of relationships between environmental and topological covariates and 348 measures of metapopulation persistence. 349

To date, metapopulation persistence in a dynamic sense has largely been determined through 350 model simulations, which quantify metapopulation persistence as the fraction of simulations 351 in which the metapopulation avoids extinction (Molofsky and Ferdy, 2005) or the mean time 352 until metapopulation extinction (Johst et al., 2002). While models may be parameterized with 353 observational data, there remains a disconnect between the theory of metapopulation persistence 354 and metapopulation dynamics in natural systems (Moilanen, 2002). By quantifying metapopulation 355 persistence using the distribution of persistence times, it is possible to characterize metapopulation 356 persistence without the necessity of metapopulation extinction. However, the fit power law 357 parameter (α) to the distribution of persistence times has some limitations. For instance, imperfect 358

detection could cause gaps that strongly influence the tail of the persistence time distribution (i.e., 359 those long persisting patches), which can alter the α parameter of the power law. Further, the 360 habitat patches which go extinct and are recolonized differentially contribute to the distribution 361 of persistence times, as they can contribute many small values, whereas persistent patches 362 contribute fewer values. The ideal measure of metapopulation persistence would incorporate 363 both information on the spatial arrangement of habitat patches and the persistence times of 364 patches. Currently, the measures of metapopulation persistence examined here rely on *either* 365 spatial patch arrangement (metapopulation capacity) or patch persistence times (power law fits). 366 Future work should attempt to bridge this gap to capture a complete view of metapopulation 367 persistence, as well as incorporating the role of self-connections of habitat patches (Zamborain-Mason 368 et al., 2017). Lastly, it is noteworthy that these measures of metapopulation persistence may be 369 independent of metapopulation stability in some situations. That is, the measures of metapopulation 370 persistence used here may not capture the ability of the metapopulation to recover from a 371 perturbation (Gilarranz et al., 2017) (but see Ovaskainen and Hanski (2002)) or targeted attack 372 (Albert et al., 2000). 373

The relationship between spatial dispersal network structure and resulting metapopulation 374 dynamics is not only of theoretical interest. Designing reserves capable of sustaining persistent 375 populations is a high priority in conservation biology and management of endangered species 376 (McCarthy et al., 2004; Nicholson and Ovaskainen, 2009). For the majority of these systems, the 377 data necessary to calculate persistence time dsitributions are not available. Thus, the finding 378 of a positive relationship between structural measures of metapopulation persistence and their 379 temporal counterparts suggests that the use of spatial habitat patch arrangement in reserve 380 design is justified as a means to enhance metapopulation persistence. Beyond reserve design, 381 the arrangement of nodes in spatial networks in a fashion that maximizes persistence is of great 382 importance to the design of many different types of networks (Ebel et al., 2002; Kamra et al., 2006; 383 Rothenberg, 2001; Wu et al., 2017), including those related to transportation (e.g., highways), 384 communication (e.g., telephone service centers), disease transmission, and sensor arrays (e.g., air 385 quality towers). Providing demonstrations of the relationships between topological properties of 386

- ³⁸⁷ networks and their corresponding dynamics will further aid the creation of persistent networks.
- ³⁸⁸ Identifying these topological properties in ecological networks provides evidence for self-organization
- to promote persistence, providing insight into the structure and stability of ecological systems.

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Figure legends

Figure 1: Estimates of metapopulation persistence were based on either the structure of the interaction network (**a**) or the distribution of patch persistence times (**c**), where measures exclusively consider either landscape matrix structure or patch persistence times, respectively. Estimates of metapopulation persistence are mapped onto the set of 88 semi-independent networks in the Åland islands (**b** and **d**), illustrating the variation in metapopulation capacity in **b** and the power law fit (α) to the persistence time distribution (**d**). Grey shaded polygons correspond to networks where network statistics could not be calculated.

Figure 2: Relationships between metapopulation persistence measures – metapopulation capacity (λ) and persistence time distributions (power law fits; α) – and the mean persistence time of patches (**a** and **b**) and the mean fraction of occupied patches (**c** and **d**) for each semi-independent network (SIN). Reported statistics correspond to Spearman's partial rank correlation coefficient and associated p-value.

Figure 3: The relationship between metapopulation capacity (λ) and persistence time distributions (power law fits; α) for each semi-independent network (SIN). Error bars represent the estimated standard deviation in the α parameter, and point size is proportional to the *p*-value of the goodness of fit test for the power law fit to the persistence time distribution. Reported statistics correspond to Spearman's rank correlation coefficient and associated *p*-value.

Figure 4: Spearman's correlation coefficients between network (in blue) and environmental (in green) covariates, and both measures of metapopulation persistence ((metapopulation capacity λ and persistence time distribution fits α). The grey line corresponds to an equally strong correlation with both measures of metapopulation persistence. The majority of covariates are close to this line, signaling a similar relationship between each covariate and the two persistence measures.

Figures









Metapopulation capacity (λ_i)





Appendix A: Supplementary Materials

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Properties of semi-independent networks

The semi-independent networks (SINs) examined in this manuscript were made up of a wide range of habitat patches in terms of overall number of patches per SIN (Figure A1) and area of each patch (Figure A6). We view this as an overall strength, as this likely increases the chances that our findings are robust to other metapopulation systems.



Figure A1: The distribution of the number of habitat patches for each semi-independent network (SIN) in the Åland islands system.

Power law fits to patch persistence times

Best fit power law distributions to the empirical data different greatly in their best fit parameterizations 545 of *xmin* – corresponding to the lower threshold persistence time in the power law fit (Figure A2)– 546 and α – corresponding to the scaling or shape parameter of the power law (Figure A3). Further, 547 the standard deviation in the best fit parameter for each semi-independent network tended to be 548 fairly large as xmin and α became larger (Figure A4), demonstrating a clear relationship between 549 the two fit parameters. Finally, the result of the best fit power laws to the persistence time 550 distribution for a sample of the semi-independent networks demonstrates both the difficulty in 551 fitting some distributions (e.g., SIN 107 in Figure A5) and the qualitative goodness of fit to other 552 persistence time distributions (e.g., SIN 17,22,and 3 in Figure A5). 553



Figure A2: The distribution of xmin values for the set of semi-independent networks, corresponding to the lower threshold for the power law fitting procedure, optimized using the Kolmogorov-Smirnoff statistic.



Figure A3: The distribution of power law fit scaling parameter (α) for the set of semi-independent networks. The majority of values fall between 2 and 3, as suggested in other empirical systems (Clauset et al., 2009).



Figure A4: The relationship between the power law fit xmin and scaling parameter (α). Points are best fit values, and error bars correspond to standard deviations in parameter estimates.



Figure A5: A set of nine of the patch persistence time distributions (bars) and power law fits (black lines, values of power law α parameter in black), where each panel corresponds to a single SIN (SIN identifier in color).

Without considering patch area in the landscape matrix

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Patch area was included in quantification of links between habitat patches. This assumes that 555 larger habitat patches are more strongly connected than smaller habitat patches. The putative 556 mechanism underlying this is that larger habitat patches support larger populations, and dispersal 557 is density-dependent, resulting in a larger number of emigrants from large habitat patches. Patch 558 area was quite variable in the set of habitat patches and SINs examined (Figure A6), suggesting 559 that patch area may play a large role in estimating entries of the landscape matrix M. Here, 560 we quantify metapopulation capacity based on a landscape matrix (M) without the influence of 561 patch area, finding strikingly similar results compared to when patch area was included (Figure 562 A7 and A8). 563



Figure A6: The distribution of habitat patch areas (log+1 transformed) in the Åland islands.



Figure A7: The relationship between metapopulation capacity (λ) and persistence time distributions (power law fits; α) for each semi-independent network (SIN). Error bars represent the estimated standard deviation in the α parameter, and point size is proportional to the *p*-value of the goodness of fit test for the power law fit to the persistence time distribution. Reported statistics correspond to Spearman's rank correlation coefficient and associated *p*-value.



Figure A8: Spearman's correlation coefficients between network (in blue) and environmental (in green) covariates, and both measures of metapopulation persistence ((metapopulation capacity λ and persistence time distribution fits α). The grey line corresponds to an equally strong correlation with both measures of metapopulation persistence. The majority of covariates are close to this line, signaling a similar relationship between each covariate and the two persistence measures.

Resource availability and grazing pressure

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Numerous relationships existed between environmental variables and metapopulation capacity, 565 despite metapopulation capacity being based solely on the landscape matrix (M). Given this, why 566 is metapopulation capacity often related to environmental variables? One potential reason is that 567 collinearity among patch area and environmental variables allows environmental variation to be 568 captured by metapopulation capacity. This can be observed in the relationship between patch 569 area and resource availability (r = 0.30, p = 0.004), and in the subsequent relationship between 570 resource availability and grazing pressure (r = -0.37, p = 0.0003; Figure A9). However, as noted 571 in the main text, this explanation does not account for the fact that environmental correlations to 572 metapopulation capacity (Figure A8) were maintained when patch area was removed from the 573 estimation of the landscape matrix (M). 574



Figure A9: The relationship between mean resource availability – quantified as the mean of the sum of *V. spicata* and *P. lanceolata* abundance values across the sampling period – and mean grazing pressure over the same time period.